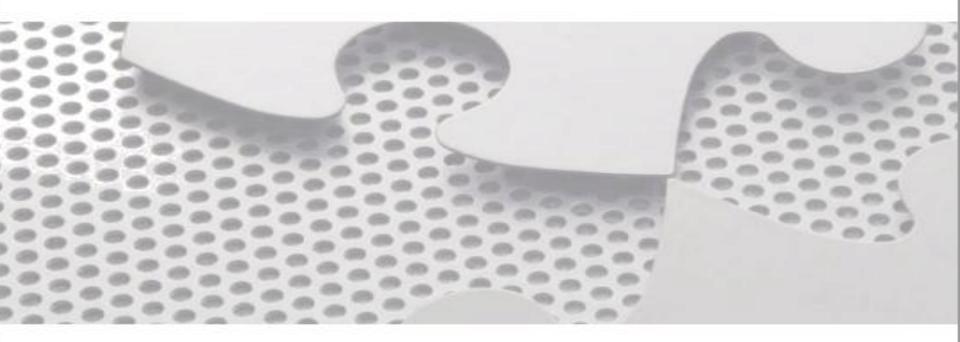
# Programming Languages Third Edition



Chapter 8 Data Types

#### Objectives

- Understand data types and type information
- Understand simple types
- Understand type constructors
- Be able to distinguish type nomenclature in sample languages
- Understand type equivalence

#### Objectives (cont'd.)

- Understand type checking
- Understand type conversion
- Understand polymorphic type checking
- Understand explicit polymorphism
- Perform type checking in TinyAda

#### Introduction

- Every program uses data, either explicitly or implicitly, to arrive at a result
- Data type: the basic concept underlying the representation of data in programming languages
- Data in its most primitive form is simply a collection of bits
  - This does not provide the kinds of abstraction necessary for large programs
- Programming languages include a set of simple data entities and mechanisms for constructing new ones

#### Introduction (cont'd.)

- Machine dependencies are often part of the implementation of these abstractions
- Finitude of data:
  - In mathematics, integer set is infinite
  - In hardware, there is always a largest and smallest integer
- Much disagreement among language designers on the extent to which type information should be made explicit and used to verify program correctness

#### Introduction (cont'd.)

- Reasons to have some form of static typechecking:
  - Execution efficiency: allows compilers to allocate memory efficiently
  - Translation efficiency: static types allow the compiler to reduce the amount of code to be compiled
  - Writability: allows many common programming errors to be caught early
  - Security and reliability: reduces the number of execution errors

#### Introduction (cont'd.)

- Reasons to have some form of static type-checking (cont'd.):
  - Readability: explicit types help to document data design
  - Remove ambiguities: explicit types can be used to resolve overloading
  - Design tool: explicit types highlight design errors and show up as translation-time errors
  - Interface consistency and correctness: explicit data types help in verification of large programs
- **Data type**: the basic abstraction mechanism

# Data Types and Type Information

- Program data can be classified according to their types
- Type name represents the possible values that a variable of that type can hold and the way those values are represented internally
- Data type (definition 1): a set of values
  - int  $x_i$ ; means the same as value of  $x \in Integers$
- **Data type** (definition 2): a set of values, together with a set of operations on that values having certain properties

- A data type is actually a mathematical algebra Programming Languages, Third Edition

- **Type checking**: the process a translator goes through to determine whether type information in a program is consistent
- **Type inference**: the process of attaching types to expressions
- Type constructors: mechanisms used with a group of basic types to construct more complex types
  - Example: Array takes a base type and a size or range indication and constructs a new data type
- User-defined types: types created using type constructors

- **Type declaration** (or **type definition**): used to associate a name with a new data type
- Anonymous type: a type with no name
   Can use typedef in C to assign a name
- **Type equivalence**: rules for determining if two types are the same
- **Type system**: methods for constructing types, the type equivalence algorithm, type inference rules, and type correctness rules

- Strongly typed: a language that specifies a statically applied type system that guarantees all data-corrupting errors will be detected at the earliest possible point
  - Errors are detected at translation time, with a few exceptions (such as array subscript bounds)
- Unsafe programs: programs with data-corrupting errors
- Legal programs: proper subset of safe programs; those programs accepted by a translator

- Weakly-typed language: one that has loopholes
  that may allow unsafe programs
- Untyped (or dynamically typed) languages: languages without static type systems
  - All safety checking is performed at execution time
- **Polymorphism**: allows names to have multiple types while still permitting static type checking

# Simple Types

- **Predefined types**: those types supplied with a language, from which all other types are constructed
  - Generally specified using either keywords or predefined identifiers
  - May include some variations on basic types, such as for numeric types
- **Simple types**: have no other structure than their inherent arithmetic or sequential structure
  - Usually includes predefined types
  - Includes enumerated types and subrange types

- Enumerated types: sets whose elements are named and listed explicitly
  - Example: In C: enum Color {Red, Green, Blue};
  - Are ordered in most languages: order in which the values are listed is important
  - Most languages include a predefined successor and predecessor operation for enumerated types
  - No assumptions are made about how the listed values are represented internally

```
with Text IO; use Text IO;
(2) with Ada.Integer Text IO; use Ada.Integer Text IO;
(3) procedure Enum is
(4)
      type Color Type is (Red, Green, Blue);
(5) -- define Color IO so that Color Type values can be -- printed
(6) package Color IO is new Enumeration IO(Color Type);
(7) use Color IO;
(8) x : Color Type := Green;
(9) begin
(10) x := Color Type'Succ(x); -- x is now Blue
(11) x := Color Type'Pred(x); -- x is now Green
(12) put(x); -- prints GREEN
(13) new line;
(14) end Enum;
```

#### Figure 8.1 An Ada program demonstrating the use of an enumerated type

#### (1) #include <stdio.h>

```
(2) enum Color {Red,Green,Blue};
(3) enum NewColor {NewRed = 3, NewGreen = 2, NewBlue = 2};
(4) main() {
(5) enum Color x = Green; /* x is actually 1 */
(6) enum NewColor y = NewBlue; /* y is actually 2 */
(7) x++; /* x is now 2, or Blue */
(8) y--; /* y is now 1 -- not even in the enum */
(9) printf("%d\n",x); /* prints 2 */
(10) printf("%d\n",y); /* prints 1 */
(11) return 0;
(12) }
```

Figure 8.2 A C program demonstrating the use of an enumerated type, similar to Figure 8.1

- Subrange types: contiguous subsets of simple types specified by giving least and greatest elements
  - Example: type Digit\_Type is range 0..9;
- Ordinal types: types that exhibit a discrete order on the set of values
  - All numeric integer types are ordinal types
  - Always have comparison operators
  - Often have successor and predecessor operations
- Real numbers are not ordinal; they have no successor and predecessor operations Programming Languages, Third Edition

- Allocation schemes are usually dependent on the underlying hardware for efficiency
- IEEE 754 standard tries to define standard representations

#### Type Constructors

- Since data types are sets, set operations can be used to construct new types from existing ones
- Set operations that can be used include Cartesian product, union, powerset, function set, and subset
   These set operations are called type constructors
- Example: subrange type is formed using subset construction
- There are type constructors that do not correspond to mathematical set constructions, and some set operations that do not correspond to type constructors

#### **Cartesian Product**

 Given two sets U and V, the Cartesian product (or cross product) consists of all ordered pairs of elements from U and V:

 $U \times V = \{(u, v) \mid u \text{ is in } U \text{ and } v \text{ is in } V\}$ 

 In many languages, the Cartesian product type constructor is available as the record or structure construction

#### Cartesian Product (cont'd.)

• Example: In C, this struct declaration constructs the Cartesian product of type int × char × double.

```
struct IntCharReal{
    int i;
    char c;
    double r;
};
```

#### Cartesian Product (cont'd.)

- Difference between a Cartesian product and a record structure:
  - In a record structure, components have names
  - In a Cartesian product, they are referred to by position
- Most languages consider component names to be part of the type defined by a record structure
- **Tuple**: a purer form of record structure in ML that is essentially identical to the Cartesian product

```
type IntCharReal = int * char * real;
```

#### Cartesian Product (cont'd.)

- Class: a data type found in object-oriented languages
  - Includes member functions or methods
  - Closer to the second definition of data type, which includes functions that act on the data

# Union

- Union of two types: formed by taking the set theoretic union of the sets of their values
- Two varieties
  - Discriminated unions: a tag or discriminator is added to the union to distinguish the type of its elements
  - Undiscriminated unions: lack the tags; assumptions must be made about the type of any value
- A language with undiscriminated unions has an unsafe type system

- In C and C++, the union type constructor creates undiscriminated unions
- Example:

```
union IntOrReal{
    int i;
    double r;
};
```

- If x is a variable of type union IntOrReal, x.i is interpreted as an int, and x.r is interpreted as a double

 Ada has a completely safe union mechanism called a variant record

```
type Disc is (IsInt, IsReal);
type IntOrReal (which: Disc) is
record
    case which is
      when IsInt => i: integer;
      when IsReal => r: float;
    end case;
end record;
...
x: IntOrReal := (IsReal,2.3);
```

 In ML, declare an enumeration with the vertical bar for "or":

datatype IntOrReal = IsInt of int | IsReal of real;

• Then use pattern matching:

```
fun printInt x =
   (print("int: "); print(Int.toString x); print("\n"));
fun printReal x =
   (print("real: "); print(Real.toString x); print("\n"))
fun printIntOrReal x =
   case x of
    IsInt(i) => printInt i |
    IsReal(r) => printReal r ;
```

- The tags IsInt and IsReal in ML are called data constructors, since they construct data of each kind within a union
- Unions are useful in reducing memory allocation requirements for structures when different data items are not needed simultaneously
- Unions are not needed in object-oriented languages
  - Use inheritance to represent different nonoverlapping data requirements

#### Subset

- A subset in math is specified by giving a rule to distinguish its elements
- Similar rules can be given in programming languages to establish new types as subsets of known types
- Ada has a subtype mechanism: subtype IntDigit\_Type is integer range 0..9;
- Variant parts of records can be fixed using subtype subtype IRInt is IntOrReal(IsInt); subtype IRReal is IntOrReal(IsReal);

## Subset (cont'd.)

- Such subset types inherit operations from their parent types
  - Most languages do not allow the programmer to specify which operations are inherited and which are not
- Inheritance in object-oriented languages can also be viewed as a subtype mechanism
  - With a great deal more control over which operations are inherited

#### Arrays and Functions

- The set of all functions f:U→V can give rise to a new type in two ways:
  - Array type
  - Function type
- If U is an ordinal type, the function f can be thought of as an array with index type U and component type V
  - If i is in U, then f(i) is the i<sup>th</sup> component of the array
  - Whole function can be represented by the sequence or tuples of its values (f(low),..., f(high))

- Arrays are sometimes called **sequence types**
- Typically, array types can be defined with or without sizes
  - To define a variable of an array type, usually necessary to specify size at translation time since arrays are normally allocated statically
- In C, the size of an array must be a literal, not a computed constant
- Cannot dynamically define an array size in C or C++

- C allows arrays without specified size to be parameters to functions (they are essentially pointers), but the size must be supplied
  - Size of the array is not part of the array in C or C++

```
int array_max (int a[], int size){
    int temp, i;
    assert(size > 0);
    temp = a[0];
    for (i = 1; i < size; i++)
        if (a[i] > temp) temp = a[i];
    return temp;
}
```

- In Java, arrays are always dynamically (heap) allocated, and the size can be dynamically specified (but cannot change)
  - Size is stored when an array is allocated in its length property

```
import java.io.*;
import java.util.Scanner;
public class ArrayTest{
   static private int array max(int[] a) { // note location of []
      int temp;
      temp = a[0];
     // length is part of a
      for (int i = 1; i < a.length; i++)
         if (a[i] > temp) temp = a[i];
     return temp;
   public static void main (String args[]) { // this placement of [] also
                                              // allowed
      System.out.print("Input a positive integer: ");
      Scanner reader = new Scanner(System.in));
      int size = reader.nextInt();
      int[] a = new int[size] ; // Dynamic array allocation
      for (int i = 0; i < a.length; i++) a[i] = i;
      System.out.println(array max(a));
```

Figure 8.3 A Java program demonstrating the use of arrays

- Ada allows array types declared without a size, called unconstrained arrays, but requires a size when array variables are declared
- Multidimensional arrays are also possible
- Arrays are perhaps the most widely used type constructor
- Implementation is extremely efficient
  - Space is allocated sequentially in memory
  - Indexing is performed by an offset calculation from the starting address

#### Arrays and Functions (cont'd.)

- For multidimensional arrays, must decide which index to use first in the allocation scheme
  - Row-major form: all values of the first row are allocated first, then all values of the second row, etc.
  - Column-major form: all values of the first column are allocated first, then all values of the second column, etc.
- Functional languages usually do not supply an array type; most use the **list** in place of an array
  - Scheme has a vector type

#### Arrays and Functions (cont'd.)

- General function and procedure types can be created in some languages
- Example: in C, define a function type from integers to integers: typedef int (\*IntFunction)(int);
  - Use this type for variables or parameters:

```
int square(int x) { return x*x; }
IntFunction f = square;
int evaluate(IntFunction g, int value)
{ return g(value); }
...
printf("%d\n", evaluate(f,3)); /* prints 9 */
```

#### Arrays and Functions (cont'd.)

- In ML, you can define a function type:
   type IntFunction = int -> int;
  - Use it in a similar fashion:

```
fun square (x: int) = x * x;
val f = square;
fun evaluate (g: IntFunction, value: int) = g value;
...
evaluate(f,3); (* evaluates to 9 *)
```

#### Pointers and Recursive Types

- **Reference** or **pointer** constructor: constructs the set of all addresses that refer to a specified type
  - Does not correspond to a set operation
- Example in C: typedef int\* IntPtr;
  - Constructs the type of all addresses where integers are stored
- Pointers are implicit in languages that perform automatic memory management
  - In Java, all objects are implicitly pointers that are allocated explicitly (using the new operator) but deallocated automatically by garbage collection

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#### Pointers and Recursive Types (cont'd.)

- **Reference**: address of an object under control of the system that cannot be used as a value or operated on in any way (except copying)
- **Pointer**: can be used as a value and manipulated by the programming
- References in C++ are created by a postfix & operator
- **Recursive type**: a type that uses itself in its declaration

## Pointers and Recursive Types (cont'd.)

- Recursive types are important in data structures and algorithms
  - Represent data whose size and structure is not known in advance and may change as computation proceeds
  - Examples: lists and binary trees
- Consider this C-like declaration of lists of characters:

```
struct CharList{
    char data;
    struct CharList next; /* not legal C! */
};
```

#### Pointers and Recursive Types (cont'd.)

- C requires that each data type have a fixed maximum size determined at translation time
  - Must use pointer to allow manual dynamic allocation to overcome this problem

```
struct CharListNode{
    char data;
    struct CharListNode* next; /* now legal */
};
typedef struct CharListNode* CharList;
```

 Each individual element in a CharListNode now has a fixed size, and they can be strung together to form a list of arbitrary size

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#### Data Types and the Environment

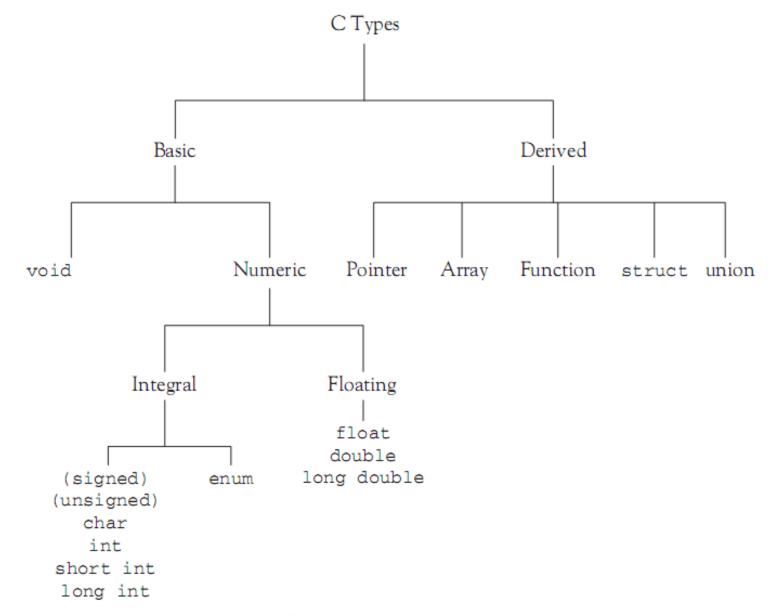
- Pointer types, recursive types, and general function types require space to be allocated dynamically
  - Require fully dynamic environments with automatic allocation and deallocation (garbage collection)
  - Found in the functional languages and the more dynamic object-oriented languages
- More traditional languages (C++ and Ada) restrict these types so that a heap (a dynamic space under programming control) is sufficient
- Environment issues will be discussed in full in Chapter 10

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# Type Nomenclature in Sample Languages

- Various language definitions use different and confusing terminology to define similar things
- This section gives a brief description of the differences among three languages: C, Java, and Ada

- Simple data types are called **basic types**, including:
  - void type
  - Numeric types:
    - Integral types, which are ordinal (12 possible kinds)
    - Floating types (3 possible kinds)
- Integral types can be signed or unsigned
- Derived types: constructed using type constructors



#### Figure 8.5 The type structure of C

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#### Java

- Simple types are called primitive types, including:
  - Boolean (not numeric or ordinal)
  - Numeric, including:
    - Integral (ordinal)
    - Floating point
- Reference types: constructed using type constructors
  - Array
  - Class
  - Interface

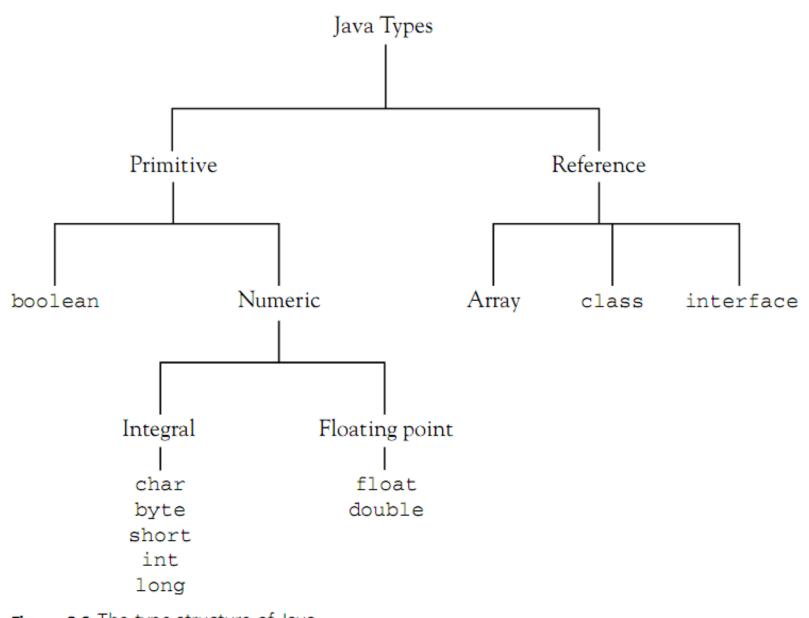
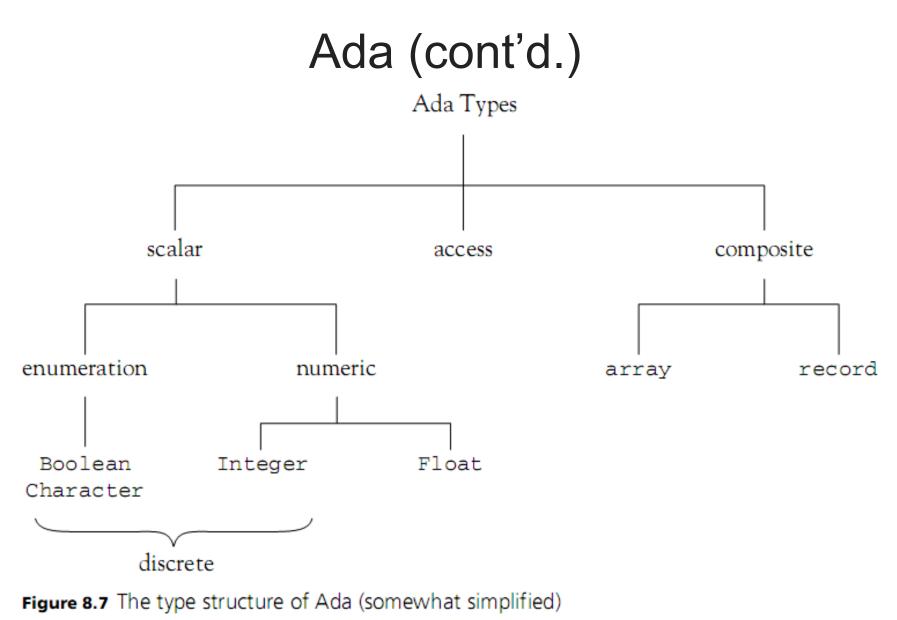


Figure 8.6 The type structure of Java Programming Languages, Third Edition

#### Ada

- Ada has a rich set of types
  - Simple types are called **scalar types**
  - Ordinal types are called **discrete types**
  - Numeric types include real and integer types
  - Pointer types are called access types
  - Array and record types are called composite types



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#### Type Equivalence

- **Type equivalence**: when are two types the same?
- Can compare the sets of values as sets
  - Are the same if they contain the same values
- Structural equivalence: two data types are the same if they have the same structure
  - Built in the same way using the same type constructors from the same simple types
  - This is one of the principal forms of type equivalence in programming languages

#### • Example:

- Rec1 and Rec2 are structurally equivalent
- Rec1 and Rec3 are not structurally equivalent (char and int fields are reversed)

```
struct Rec1{
   char x;
   int y;
   char z[10];
};
struct Rec2{
   char x;
   int y;
   char z[10];
};
struct Rec3{
   int y;
   char x;
   char z[10];
};
```

- Structural equivalence is relatively easy to implement (except for recursive types)
  - Provides all the information needed to perform error checking and storage allocation
- To check structural equivalence, a translator may represent types as trees and check equivalence recursively on subtrees
- Questions still arise over how much information is included in a type under the application of a type constructor

• Example: are A1 and A2 structurally equivalent?

```
typedef int A1[10];
typedef int A2[20];
```

- Yes, if size of the index set is not part of an array type
- Otherwise, no
- Similar question arises regarding member names of structures

• Example: Are these two structures structurally equivalent?

<pre>struct RecA{</pre>	<pre>struct RecB{</pre>
char x;	char a;
int y;	int b;
};	};

- If structures are considered to be just Cartesian products, then yes
- They are typically not considered equivalent, because variables of different structures would have to use different names to access member data

- **Type names** in declarations may or may not be given explicitly
  - In C, variable declarations can use anonymous types
  - Names can also be given right in structs and unions, or by using a typedef
- Structural equivalence when type names are present can be done by simply replacing each name by its associated type expression in its declaration (except for recursive types)

- Example: in C code
  - Variable a has two names:
     struct RecA and RecA
     (given by the typedef)
  - Variable b has only the name RecB (the struct name was left blank)
  - Variable c has no type
     name at all (only an internal name not usable by the programmer)

```
struct RecA{
   char x;
   int y;
 a;
typedef struct RecA RecA;
typedef struct{
   char x;
   int y;
} RecB;
RecB b;
struct{
   char x;
   int y;
  C;
```

 Structural equivalence by replacing names with types can lead to infinite loops in a type checker when applied to recursive types

```
typedef struct CharListNode* CharList;
typedef struct CharListNode2* CharList2;
struct CharListNode{
    char data;
    CharList next;
};
struct CharListNode2{
    char data;
    CharListNode2{
    char data;
    CharList2 next;
};
```

- Name equivalence: two types are the same only if they have the same name
  - Easier to implement than structural equivalence, as long as every type has an explicit name
  - Two types are equivalent only if they are the same name
  - Two variables are type equivalent only if their declarations use exactly the same type name

- Example: in C code:
  - a, b, c, and d are structurally
     equivalent
  - a and c are name equivalent,
     and not name equivalent to b
     or d
  - b and d are not name
     equivalent to any other
     variable

```
struct RecA{
   char x;
   int y;
};
typedef struct RecA RecA;
struct RecA a;
RecA b;
struct RecA c;
struct{
   char x;
   int y;
 d;
```

- Ada implements a very pure form of name equivalence
  - Requires type names in variable and function declarations in virtually all cases
- C uses a form of type equivalence that falls between name and structural equivalence:
  - Name equivalence for structs and unions
  - Structural equivalence for everything else
- Pascal is similar to C, except that almost all type constructors lead to new, inequivalent types

- Java's approach is simple:
  - It has no typedefs
  - class and interface declarations implicitly create new type names, and name equivalence is used for these types
  - Arrays use structural equivalence, with special rules for establishing base type equivalence

# Type Checking

- **Type checking**: the process by which a translator verifies that all constructs are consistent
  - Applies a type equivalence algorithm to expressions and statements
  - May vary the use of the type equivalence algorithm to suit the context
- Two types of type checking:
  - Dynamic: type information is maintained and checked at runtime
  - Static: types are determined from the text of the program and checked by the translator

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- In a strongly typed language, all type errors must be caught before runtime
  - These languages must be statically typed
  - Type errors are reported as compilation error messages that prevent execution
- A language definition may not specify whether dynamic or static typing is used

- Example1:
  - C compilers apply static type checking during translation, but C is not strongly typed since many inconsistencies do not cause compilation errors
  - C++ adds strong type checking, but mainly in the form of compiler warnings rather than errors, which do not prevent execution

- Example 2:
  - Scheme is a dynamically typed language, but types are rigorously checked
  - Type errors cause program termination
  - No types in declarations and no explicit type names
  - Variables have no predeclared types, but take on the type of the value they possess

- Example 3:
  - Ada is a strongly typed language
  - All type errors cause compilation error messages
  - Certain errors, like range errors in array subscripting, cannot be caught prior to execution
  - Such errors cause exceptions that will cause program termination if not handled by the program

- **Type inference**: types of expressions are inferred from the types of their subexpressions
  - Is an essential part of type checking
- Type-checking rules and type inference rules are often intermingled
  - They also have a close interaction with the type equivalence algorithm
- Type inference and correctness rules are one of the most complex parts of the semantics of a language

#### Type Compatibility

- Two different types that may be considered correct when combined in certain ways are called **compatible** 
  - In Ada, any two subranges of the same base type are compatible
  - In C and Java, all numeric types are compatible (and conversions are performed)
- Assignment compatibility: the left and right sides of an assignment statement are compatible when they are the same type
  - Ignores that the left side must be an I-value and the right side must be an r-value

#### Type Compatibility (cont'd.)

- Assignment compatibility can include cases where both sides do not have the same type
- In Java, x=e is legal when e is a numeric type whose value can be converted to the type of x without loss of information

# Implicit Types

- Implicit types: types that are not explicitly given in a declaration
  - The type must be inferred by the translator, either from context information or from standard rules
- In C, variables are implicitly integers if no type is given, and functions implicitly return an integer value if no return type is given
- In Pascal, named constants are implicitly typed by the literals they represent
- Literals are the major example of implicitly typed entities

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# Overlapping Types and Multiply-Typed Values

- Two types may overlap, with values in common
- Although preferable for types to be disjoint, this would eliminate the ability to create subtypes through inheritance in object-oriented languages
- In C, types like unsigned int and int overlap
- In C, the literal 0 is a value for every integral type, a value of every pointer type, and represents the null pointer
- In Java, the literal value null is a value of every reference type

# **Shared Operations**

- Each type is associated, usually implicitly, with a set of operations
- Operations may be shared among several types or have the same name as other operations that may be different
- Example: + operator can be real addition, integer addition, or set union
- Overloaded operation: the same name is used for different operations
  - Translator must decide which operation is meant based on the types of the operands

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# Type Conversion

- **Type conversion**: converting from one type to another
  - Can be built into the type system to happen automatically
- Implicit conversion (or coercion): inserted by the translator
- Widening conversion: target data type can hold all of the converted data without loss of data
- Narrowing conversion: conversion may involve a loss of data

- Implicit conversion:
  - Can weaken type checking so that errors may not be caught
  - Can cause unexpected behavior if the conversion is done in a different way than the programmer expects
- Explicit conversion (or cast): conversion directives are written into the code
  - Conversions are documented in the code
  - Less likelihood of unexpected behavior
  - Makes it easier for the translator to resolve overloading

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• Example In C++:

```
double max (int, double);
double max (double, int);
max(2,3)
```

- Ambiguous, because of the possible implicit conversions from int to double on either first or second parameter
- Java only permits widening implicit conversions for arithmetic types
- C++ emits warning messages for narrowing

- Explicit casts need to be somewhat restricted
   Often to simple types, or just arithmetic types
- If casts are permitted for structured types, they must have identical sizes in memory
  - Allows translation to reinterpret the memory as a different type
- Example: in C, malloc and free functions are declared using a generic pointer or anonymous pointer type void\*
- Object-oriented languages allow conversions from subtypes to supertypes and back in some cases

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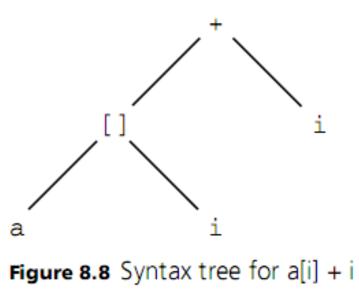
- Alternative to casts is to use predefined or library functions to perform conversions
  - Ada uses attribute functions to allow conversions
  - Java contains functions like toString to convert from int to String and parseInt to convert from String to int
- Undiscriminated unions can hold values of different types
  - With no discriminant or tag, a translator cannot distinguish values of one type from another

# Polymorphic Type Checking

- Most statically typed languages required that explicit type information be given for all names in declarations
- It is possible to determine types of names without explicit declaration:
  - Can collect information on the uses of a name and infer the type from the set of all uses
  - Can declare a type error because some of the uses are incompatible with others
- This type inference and type checking is called Hindley-Milner type checking

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- Example in C code: a [i] + i.
  - a must be declared as an array of integers, and i as an integer, giving an integer result
- Type checker starts out with this tree:



Types of the names (leaf nodes) are filled in from declarations

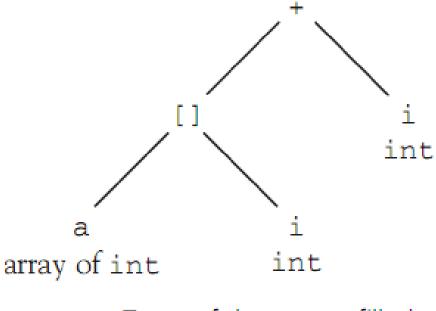


Figure 8.9 Types of the names filled in from the declarations

- Type checker now checks the subscript node (labeled [])
  - Left operand must be an array
  - Right operand must be an int
  - Inferred type of the subscript node is the component type of the array int

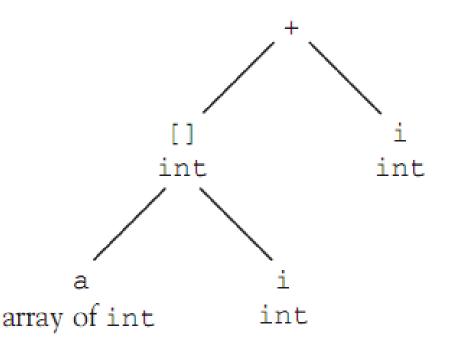


Figure 8.10 Inferring the type of the subscript node

- + node type is checked
  - Both operands must have the same type
  - This type must have a+ operation
  - Result is the type of the operands - int

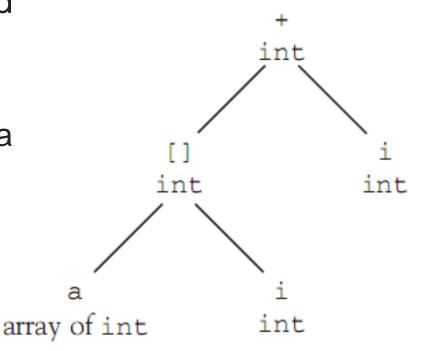


Figure 8.11 Inferring the type of the + node

• Example: in C code:

a[i] + i.

- What if the declarations of a and i were missing?
- Type checker would first assign type variables to all names that do not yet have types

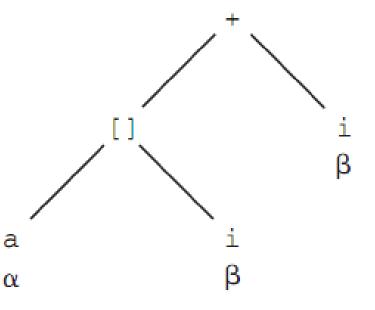


Figure 8.12 Assigning type variable to names without types

- Type checker now checks the subscript node
  - Infers that a must be an array
  - Infers that I must an int
  - Replaces β with
     int in the entire
     tree

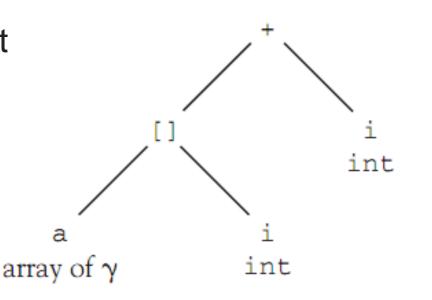


Figure 8.13 Inferring the type of the variable a

 Type checker now concludes that the subscript node is type correct and has the type γ

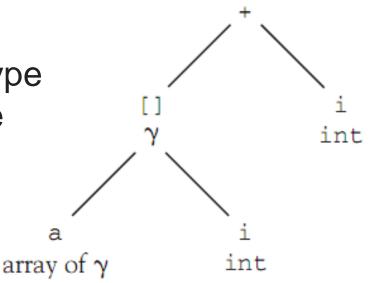


Figure 8.14 Inferring the type of the subscript node

- + node type is checked
  - Concludes that γ
     must be type int
  - Replaces γ
     everywhere by int
- This is the basic form of operation of Hindley-Milner type checking

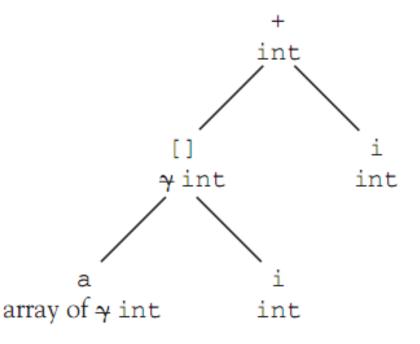


Figure 8.15 Substituting int for the type variable

 Once a type variable is replaced by an actual type, all instances of that variable name must be updated with the new type

- Called instantiation of type variables

- **Unification**: when type expressions for variables can change for type checking to succeed
  - Example array of  $\alpha$  and array of  $\beta$ : we need to have  $\alpha == \beta$ , so  $\beta$  must be changed to  $\alpha$  everywhere it occurs
  - Is a kind of pattern matching

- Unification involves three cases:
  - Any type variable unifies with any type expression (and is instantiated to that expression)
  - Any two type constants unify only if they are the same type
  - Any two type constructions (such as array or struct) unify only if they are applications of the same type constructor and all of their component types also recursively unify

- Hindley-Milner type checking advantages:
  - Simplifies the amount of type information the programmer must write
  - Allows types to remain as general as possible while still being strongly checked for consistency
- Hindley-Milner type checking implicitly implements
   polymorphic type checking
- Array of α is a set of infinitely many types, called parametric polymorphism
  - Hindley-Milner uses implicit parametric polymorphism

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- Sometimes called ad hoc polymorphism to distinguish it from overloading
- Pure polymorphism (or subtype polymorphism): when objects that share a common ancestor also either share or redefine operators that exist for the ancestor
- **Monomorphic**: describes a language that exhibits no polymorphism

- Polymorphic functions are real goal of parametric polymorphism and Hindley-Milner type checking
- Example:

```
int max (int x, int y) {
    return x > y ? x : y;
```

- Body is the same if int is replaced by any other arithmetic type
- Could add a new parameter representing the >

```
int max (int x, int y, int (*gt)(int a, int b) ) {
   return gt(x,y) ? x : y;
}
```

• In C-like syntax:

```
max (x, y, gt) {
    return gt(x,y) ? x : y;
}
```

• In ML legal syntax, this becomes:

fun max (x, y, gt) = if gt(x, y) then x else y;

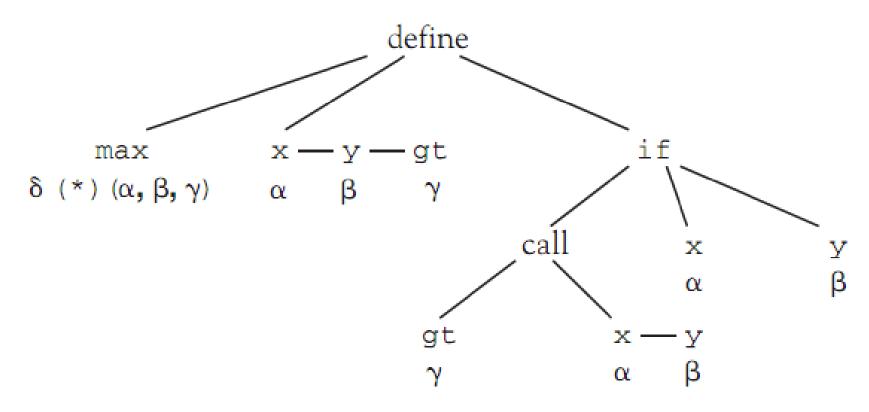


Figure 8.16 A syntax tree for the function max

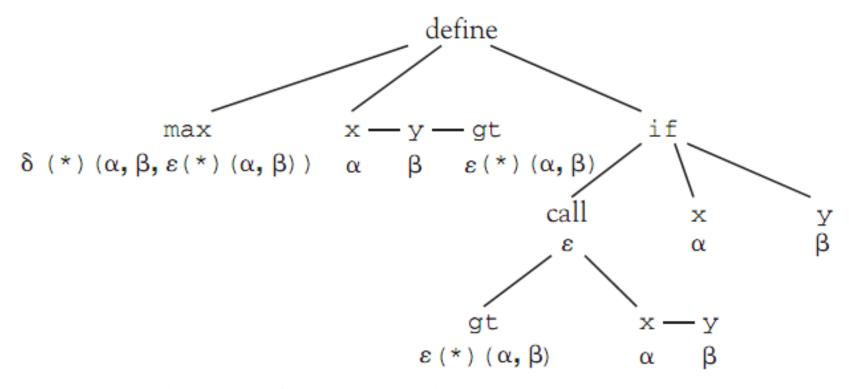
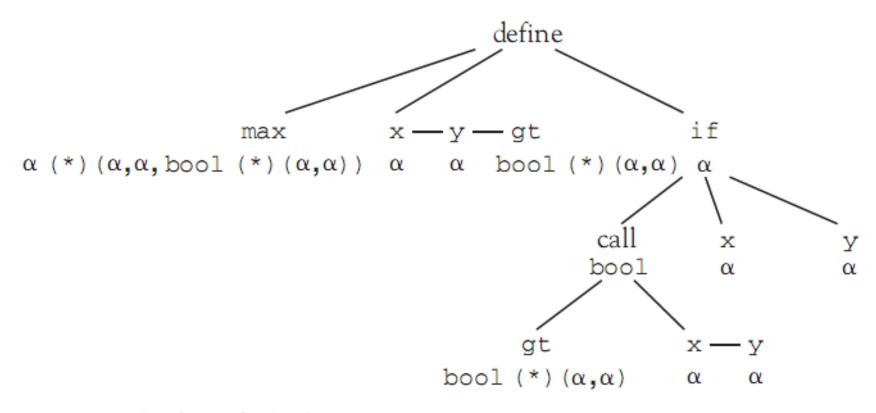


Figure 8.17 Substituting for a type variable



#### Figure 8.18 Further substitutions

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- Can now use max in any situation where the actual types unify
- If we provide these definitions in ML: fun gti (x:int,y) = x > y; fun gtr (x:real,y) = x > y; fun gtp ((x,y), (z,w)) = gti (x,z); – We can call max function as follows:

```
max(3,2,gti); (* returns 3 *)
max(2.1,3.2,gtr); (* returns 3.2 *)
max((2,"hello"),(1,"hi"),gtp); (* returns (2,"hello") *)
```

- Most general type possible for max function, called its principal type, is: α (\*) (α, α, bool (\*) (α, α))
- Each call to max specializes this principle type to a monomorphic type
  - May also implicitly specialize the types of the parameters
- Any polymorphically typed object passed into a function as a parameter must have a fixed specialization for the duration of the function

This restriction is called **let-bound polymorphism**

- Two problems complicate Hindley-Milner type checking:
  - Let-bound polymorphism
  - The occur-check problem
- Polymorphic types also have translation issues
  - Copying values of arbitrary type without knowing the type means the translator cannot determine the size of the values
  - May cause code bloat

#### Explicit Polymorphism

- Explicit parametric polymorphism: to define a polymorphic data type, the type variable must be written explicitly

- Values of type Stack can be written as: val empty = EmptyStack; (\* empty has type 'a Stack \*) val x = Stack(3, EmptyStack); (\*x has type int Stack \*)

# Explicit Polymorphism (cont'd.)

 Explicitly parameterized polymorphic data types are nothing more than a mechanism for creating user-defined type constructors

A type constructor is a function from types to types

- Construction can be expressed directly in C as a typedef
- In ML, this is done with the type construct
- C++ is a language with explicit parametric polymorphism, but without the associated implicit Hindley-Milner type checking

- Uses the **template** mechanism Programming Languages, Third Edition

#### Explicit Polymorphism (cont'd.)

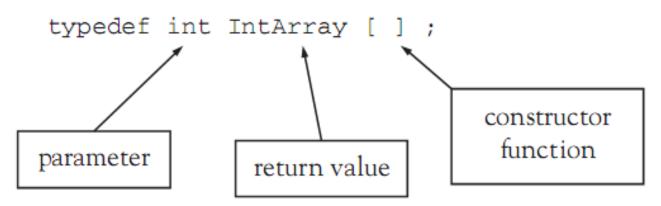


Figure 8.19 The components of a type definition in C

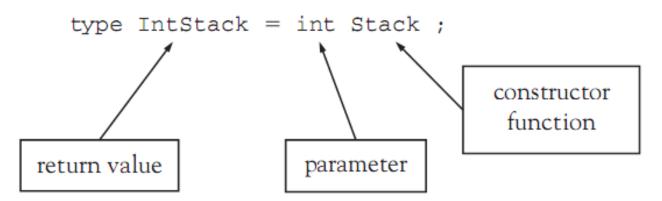


Figure 8.20: The components of a type definition in ML

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## Explicit Polymorphism (cont'd.)

- Implicitly constrained parametric polymorphism: implicitly applies a constraint to the type parameter
- Explicitly constrained parametric polymorphism: makes explicit what types of parameters are required

# Case Study: Type Checking in TinyAda

- Goals:
  - Check identifiers to ensure that they are declared before they are used
  - Check that identifiers are not declared more than once in the same block
  - Record the role of an identifier as a constant, variable, procedure, or type name

# Type Compatibility, Type Equivalence, and Type Descriptors

- TinyAda parser must:
  - Check that the type of an operand is appropriate for the operation being performed
  - Check that the name on the left side of an assignment statement is type-compatible with the expression on the right side
  - Restrict the types of certain elements of declarations, such as the index types of an array

# Type Compatibility, Type Equivalence, and Type Descriptors (cont'd.)

- TinyAda uses a loose form of name equivalence to determine type compatibility
  - For arrays and enumerations, two identifiers are type-compatible if and only if they were declared using the same type name in their declarations
  - For built-in types INTEGER, CHAR, and BOOLEAN and their programmer-defined subrange types, two identifiers are type-compatible if and only if their supertypes are name-equivalent

Type Compatibility, Type Equivalence, and Type Descriptors (cont'd.)

- **Type descriptor**: primary data structure used to represent type attributes
- Type descriptor is entered into the symbol table when the type name is introduced
  - At startup for built-in type names INTEGER, CHAR, and BOOLEAN
  - Whenever new type declarations are encountered

# The Design and Use of Type Descriptor Classes

- Type descriptor is like a variant record, containing different attributes depending on the category of the data type being described
- Each descriptor includes a type form field, with possible values of ARRAY, ENUM, SUBRANGE, and NONE, to identify the category of the data type
- Array type descriptor includes attributes for index types and element types (these attributes are also type descriptors)
- Enumeration type descriptor includes a list of symbol entries for the enumerate constant names

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# The Design and Use of Type Descriptor Classes (cont'd.)

- Type descriptors for subrange types (including INTEGER, CHAR, and BOOLEAN) include values of lower and upper bound and a type descriptor for the supertype
- There is no variant record structure in Java
  - Can model it with a TypeDescriptor class and three subclasses: ArrayDescriptor,
     SubrangeDescriptor, and EnumDescriptor

# Entering Type Information in Declarations

- Type information must be entered wherever identifiers are declared in a source program
- Type information comes from type identifiers or from a type definition
  - Type identifiers: type descriptor is available in the identifier's symbol entry
  - Type definition: a new type might be created

# Checking Types in Operands in Expressions

- The rules for TinyAda expressions give hints as to how their types should be checked
- The type of every operand must be checked, and the correct type descriptor must be returned

# Processing Names: Indexed Component References and Procedure Calls

- Syntax for TinyAda indexed component references and procedure calls is the same if the procedure expects at least one parameter
  - Must distinguish between these two types of phrases, based on the role of the leading identifier

#### **Completing Static Semantic Analysis**

- Two other types of semantic restrictions can be imposed during parsing:
  - Checking of parameter modes
  - Check that only static expressions are used in number declarations and range type definitions
- Tanya has three parameter modes:
  - Input only: with the keyword in
  - Output only: with the keyword out
  - Input/output: with the keywords in out